

#### CPSC-440 Computer System Architecture

MATLAB Review



# Matlab

- Is a numerical computing environment and 4<sup>th</sup> generation programming language
- Developed by MathWorks, MATLAB allows matrix manipulations, plotting of functions and data, implementation of algorithms, creation of user interfaces, and interfacing with programs written in other languages, including C, C++, Java, and Fortran



## Free Matlab for Students

- Available at CSUF IT website:
	- [http://www.fullerton.edu/it/students/software/m](http://www.fullerton.edu/it/students/software/matlab/) atlab/



#### Matlab Default View





#### Command Window





## Workspace Window

• Shows the variables currently available to you





## Command History Window

- Shows the commands you have entered
- Sorted by date





## Current Folder Window

• Shows the folders for the present working directory





## Present Working Directory

- Shows the current folder you are working in
- You can also use the command "pwd"





# Help Docs

- Searchable help doc
- You can also use the "help" command
- Example: help **plot**





### Creating Scripts





# Script Editor

• Instead of entering in the command window directly, you can also enter commands in the script editor and save as a m-file





## Script Editor





### Script Editor





# Getting Started



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• To enter the matrix:

$$
\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}
$$

• and store it in a variable "a", do this:

>> **a = [1 2; 3 4];**

• To redisplay the matrix, just type its name:

>> **a**

• Once you know how to enter and display matrices, it is easy to compute with them. First we will square the matrix "a":

$$
\gt > a * a
$$



• Now we'll try something a little harder. First we define a matrix b:

#### >> **b = [1 2; 0 1];**

- Then we compute the product ab: >> **a\*b**
- Finally, we compute the product in the other order:

$$
\gt>b^*a
$$



- Notice that the two products are different – Matrix multiplication is non-commmutative
- Of course, we can also add matrices:

>> **a + b** 

• Now let's store the result of this addition so that we can use it later:

 $>>$   $s = a + b$ 



• Matrices can sometimes be inverted:

>> **inv(s)**

• To check that this is correct, we compute the product of s and its inverse:

>> **s \* inv(s)** 

• The result is the unit, or identity matrix. We can also write the computation as

>> **s/s** 

- We can also write >> **s\s**
- which is the same as >> **inv(s) \* s**



• To see that these operations, left and right division, are really different, we do the following:

> >> **a/b** >> **a\b**

• Not all matrices can be inverted, or used as the denominator in matrix division:

> >> **c = [ 1 1; 1 1 ];** >> **inv(c);**

• A matrix can be inverted if and only if its determinant is nonzero:

> >> **det(a)** >> **det(c)**



# Systems of Equations

• Now consider a linear equation

```
ax + by = p
```

```
cx + dy = q
```
• We can write this more compactly as

 $AX = B$ 

- where the coefficient matrix A is
	- a b
	- c d
- the vector of unknowns is

x

$$
\boldsymbol{\mathsf{y}}
$$

• and the vector on the right-hand side is

p

- q
- If A is invertible,  $X = (1/A)B$ , or, using Matlab notation,  $X = A\setminus B$ . Let's try this out by solving  $ax = b$ with a as before and  $b = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ . Note that b is a column vector.

```
>> b = [ 1; 0 ]>> a\b
```


### Loops

- Loop Example
	- We regard x as representing (for example) the population state of an island
	- The first entry (1) gives the fraction of the population in the west half of the island, the second entry (0) give the fraction in the east half
	- $-$  The state of the population T units of time later is given by the rule  $y = ax$
	- This expresses the fact that an individual in the west half stays put with probability 0.8 and moves east with probability 0.2 (note  $0.8 + 0.2 = 1$ ), and the fact that in individual in the east stays put with probability 0.9 and moves west with probability 0.1
	- Thus, successive population states can be predicted/computed by repeated matrix multiplication

```
>> a = [ 0.8 0.1; 0.2 0.9 ]
>> x = [ 1; 0 ]>> for i = 1:20, x = a*x, end
```


# Graphing

#### **Functions of One Variable**

• To make a graph of  $y = sin(t)$  on the interval  $t = 0$  to  $t = 10$  we do the following:

>> **t = 0:.3:10;** >> **y = sin(t);** >> **plot(t,y)**

- The command  $t = 0:3:10$ ; defines a vector with components ranging from 0 to 10 in steps of 0.3
- The  $y = sin(t)$ ; defines a vector whose components are sin(0), sin(0.3), sin(0.6), etc.
- Finally, plot(t,y) use the vector of t and y values to construct the graph





# Graphing

#### **Functions of Two Variable**

• Here is how we graph the function  $z(x, y) = xe^{(-x^2 - y^2)}$ >> **[x,y] = meshgrid(-2:.2:2, -2:.2:2);**

>> **z = x .\* exp(-x.^2 - y.^2);** >> **surf(x,y,z)**

- The first command creates a matrix whose entries are the points of a grid in the square  $-2 \le x \le 2$ ,  $-2 \le y \le 2$
- The small squares which make up the grid are 0.2 units wide and 0.2 unit tall
- The second command creates a matrix whose entries are the values of the function  $z(x,y)$  at the grid points
- The third command uses this information to construct the graph





#### Common Commands and Operators

• [http://www.hkn.umn.edu/resources/files/mat](http://www.hkn.umn.edu/resources/files/matlab/MatlabCommands.pdf) lab/MatlabCommands.pdf



# Useful Tutorials

- Download MATLAB and do the following tutorials:
	- [Basic Matric Operations](http://www.mathworks.com/help/matlab/examples/basic-matrix-operations.html?prodcode=ML)
	- [Getting Started with MATLAB](http://www.mathworks.com/help/matlab/getting-started-with-matlab.html)
	- Matlab [Overview Video](http://www.mathworks.com/videos/matlab-overview-61923.html)
	- [Analyzing and Visualizing Data with MATLAB](http://www.mathworks.com/videos/analyzing-and-visualizing-data-with-matlab-70942.html)
	- [Programming and Developing Algorithms with MATLAB](http://www.mathworks.com/videos/programming-and-developing-algorithms-with-matlab-71067.html)
	- [Signal Related Videos](http://www.mathworks.com/solutions/mixed-signal-systems/devices.html)





#### CPSC-440 Computer System Architecture

Lecture 1 Introduction

# Introduction



#### Computer Architecture Computer Organization





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# Structure and Function

- Hierarchical system
	- Set of interrelated subsystems
- Hierarchical nature of complex systems is essential to both their design and their description
- Designer needs to only deal with a particular level of the system at a time
	- Concerned with structure and function at each level

#### **Structure**

- The way in which components relate to each other
- Function
	- The operation of individual components as part of the structure





#### **Function**

**+**

- A computer can perform four basic functions:
	- Data processing
	- Data storage
	- Data movement
	- Control

**Operating Environment** (source and destination of data)



Figure 1.1 A Functional View of the Computer



































## The Computer



Figure 1.3 The Computer




Figure 1.4 A Top-Down View of a Computer

![](_page_36_Picture_2.jpeg)

**There are four main structural components of the computer:**

**+**

![](_page_37_Picture_1.jpeg)

• CPU

- Controls the operation of the computer and performs its data processing functions
- Main Memory
	- Stores data
- I/O
	- Moves data between the computer and its external environment
- System Interconnection
	- Some mechanism that provides for communication among CPU, main memory, and I/O

![](_page_37_Picture_10.jpeg)

#### **CPU** Major structural components:

![](_page_38_Picture_1.jpeg)

**+**

![](_page_38_Picture_2.jpeg)

#### • Control Unit

- Controls the operation of the CPU and hence the computer
- Arithmetic and Logic Unit (ALU)
	- Performs the computer's data processing function
- Registers
	- Provide storage internal to the CPU
- CPU Interconnection
	- Some mechanism that provides for communication among the control unit, ALU, and registers

![](_page_38_Picture_11.jpeg)

#### **Questions**

- **1. What, in general terms, is the distinction between computer organization and computer architecture?**
- **2. What, in general terms, is the distinction between computer structure and computer function?**
- **3. What are the four main functions of a computer?**
- **4. List and briefly define the main structural components of a computer.**
- **5. List and briefly define the main structural components of a processor.**

![](_page_39_Picture_6.jpeg)

### HW 1

- Problems 1 to 5
- HW template with problems will be available on Canvas

![](_page_40_Picture_3.jpeg)

![](_page_41_Picture_0.jpeg)

#### CPSC-440 Computer System Architecture

#### Lecture 2 Performance Assessment

### Performance

- What we care most about…
	- How fast the computer can run a program
	- Response time or throughput
		- Response time: time to finish one single program
		- Throughput: total amount of work done in unit time

![](_page_42_Picture_6.jpeg)

## CPU Performance Equation

• CPU Time

 $CPU Time = -$ Clock cycles for a program (cycles) Clock Freq (cycles/sec)

- If we know...
	- Total Instruction Counts  $(I_c)$
	- Cycles Per Instruction (CPI)
	- Clock Frequency  $(f)$
	- Cycle Time  $(\tau)$  the inverse of the clock frequency  $(1/f)$
	- CPU Time  $(T)$ :

$$
T = \frac{I_c \times CPI}{f} = I_c \times CPI \times \tau
$$

![](_page_43_Picture_10.jpeg)

#### What if different instructions have different CPIs?

• CPU Time

$$
T = \left(\sum_{i=1}^{n} (I_i \times CPI_i)\right) \times \tau
$$

• Where  $i$  is the instruction type

• CPI

$$
CPI = \frac{\sum_{i=1}^{n} (I_i \times CPI_i)}{I_c}
$$

- IPC (Instructions Per Cycle)
	- Inverse of CPI

![](_page_44_Picture_8.jpeg)

## MIPS and MFLOPS Rates

• MIPS (Millions of Instructions Per Second) Rate

$$
MIPS Rate = \frac{I_C}{T \times 10^6} = \frac{f}{CPI \times 10^6}
$$

• MFLOPS (Millions of Floating Point Operations Per Second) Rate

**MFLOPS** Rate

# of executed floating point operations in a program

*Execution time*  $\times$  10<sup>6</sup>

![](_page_45_Picture_7.jpeg)

=

### Example

- 2 million instructions on a 400 MHz processor
- 4 major types of instructions
- What's the MIPS rate?  $CPI = 0.6 + (2 \times 0.18) + (4 \times 0.12) + (8 \times 0.1) = 2.24$  $MIPS Rate = (400 \times 10^6)/(2.24 \times 10^6) \approx 178$

![](_page_46_Picture_126.jpeg)

![](_page_46_Picture_5.jpeg)

### Improve CPU time

- Instruction count
	- ISA and compiler technology
- CPI
	- Organization and ISA
- Clock cycle time
	- Hardware technology and organization

![](_page_47_Picture_7.jpeg)

### Benchmarks

- MIPS and MFLOPS rates are inadequate to evaluate performance of processors
	- Because of differences in instruction sets, these rates are not valid means of comparing the performance of different architectures

![](_page_48_Picture_3.jpeg)

### Example

#### $A = B + C$

#### Assume all quantities in main memory

![](_page_49_Picture_99.jpeg)

- Can be compiled into one instruction
- Rated at 1 MIPS
- add mem $(B)$ , mem $(C)$ , mem $(A)$

**Reduced Instruction Set Computer (RISC)**

• Rated at 4 MIPS

load mem $(B)$ , reg $(1)$ load mem $(C)$ , reg $(2)$ add reg(1),  $reg(2)$ , reg(3) store  $reg(3)$ , mem $(A)$ 

![](_page_49_Picture_10.jpeg)

#### Standard Performance Evaluation Corporation (SPEC) Benchmark

- Benchmark Suite
	- Collection of programs
	- Provides a representative test of a computer in a particular application or area

![](_page_50_Picture_4.jpeg)

### Performance Comparison

#### **Which One is Faster?**

A is 10x faster than B for Prog P1

B is 10x faster than A for Prog P2

A is 20x faster than C for Prog P1

C is 50x faster than A for Prog P2

B is 2x faster than C for Prog P1

C is 5x faster than B for Prog P2

![](_page_51_Picture_8.jpeg)

## Total Execution Rates

- Both program A and B have equal number of instructions
- Below shows the execution rates

![](_page_52_Picture_52.jpeg)

![](_page_52_Picture_4.jpeg)

## Average Execution Rate

- What if Program A and B have a different number of instructions?
- If there are  $m$  different benchmark programs

$$
R_A = \frac{1}{m} \sum_{i=1}^{m} R_i
$$

- Where  $R_i$  is the high-level language instruction execution rate for the  $i^{th}$  benchmark program
- The throughput of a machine carrying out a number of tasks
	- The higher the rate  $(R_A)$  the better

![](_page_53_Picture_7.jpeg)

## Harmonic Mean

• Alternative to average execution rate

$$
R_H = \frac{m}{\sum_{i=1}^m \frac{1}{R_i}}
$$

- The reciprocal of the arithmetic mean of the reciprocals
- Gives the inverse of the average execution rate
- Again, the higher the rate  $(R_H)$  the better

![](_page_54_Picture_6.jpeg)

## Total Execution Time Example

The top table shows the execution rates. Assume each program has equal weight.

![](_page_55_Picture_96.jpeg)

![](_page_55_Picture_97.jpeg)

![](_page_55_Picture_4.jpeg)

SPEC Benchmark Speed Metrics

• Measures the ability of a computer to complete a single task

$$
r_i = \frac{Tref_i}{T s u t_i}
$$

- *Tref<sub>i</sub>* execution time of benchmark program *i* on the reference system
- $T_{S}ut_i$  execution time of benchmark program  $i$  on the system under test
- The larger the ratio, the higher the speed

![](_page_56_Picture_6.jpeg)

SPEC Benchmark Speed Metrics

- Example
	- A system executes a program in 934 sec.
	- The reference implementation requires 22,135 sec.

$$
\frac{22,135 \, sec}{934 \, sec} = 23.7
$$

![](_page_57_Picture_5.jpeg)

#### SPEC Benchmark Rate Metric

- Throughput/rate of a machine carrying out a number of tasks
- Multiple copies of benchmarks run simultaneously

$$
r_i = \frac{N \times Tref_i}{T_{\text{S}}}
$$

• N – number of copies of the program that are run simultaneously

![](_page_58_Picture_5.jpeg)

# SPEC Benchmark

#### Geometric Mean

- Averages ratios for all 12 integer benchmarks
- Used to determine the overall performance measure

$$
r_G = \left(\prod_{i=1}^n r_i\right)^{1/n}
$$

![](_page_59_Picture_96.jpeg)

 $(17.5 \times 14 \times 13.7 \times 17.6 \times 14.7 \times 18.6 \times 17 \times 31.3 \times 23.7 \times 9.23 \times 10.9 \times 14.7)^{1/12} = 18.5$ 

![](_page_59_Picture_7.jpeg)

### Amdahl's Law

• *Speedup in one aspect of technology/design does not result in a corresponding improvement in performance*

= Execution time bef ore enh Execution time af ter enh

![](_page_60_Picture_3.jpeg)

## Amdahl's Law Example

Single vs. Multiple processors

$$
Speedup = \frac{X}{Y} = \frac{T(1-f) + Tf}{T(1-f) + \frac{Tf}{N}} = \frac{1}{(1-f) + \frac{f}{N}}
$$
\n6. Y: Time to average pressure, an single pressure

- $X$ : Time to execute a program on a single processor
- $Y:$  Time to execute a program on N parallel processors
- $T:$  Total execution time
- $f$ : Fraction of code executed on parallel processors (no scheduling overhead)
- $(1 f)$ : Fraction of code executed on a single processor
- 1. When  $f$  is small, the use of parallel processors has little effect
- 2. As  $N \to \infty$ , speedup bound by  $1/(1-f)$ 
	- Diminishing returns for using more processors

### Amdahl's Law Example

![](_page_62_Figure_1.jpeg)

![](_page_62_Picture_2.jpeg)

![](_page_63_Picture_0.jpeg)

#### CPSC-440 Computer System Architecture

#### Lecture 3 Von Neumann Machines (IAS)

## History of Computers

#### First Generation: Vacuum Tubes

- ENIAC
	- Electronic Numerical Integrator And Computer
- Designed and constructed at the University of Pennsylvania
	- Started in 1943 completed in 1946
	- By John Mauchly and John Eckert

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- World's first general purpose electronic digital computer
	- Army's Ballistics Research Laboratory (BRL) needed a way to supply trajectory tables for new weapons accurately and within a reasonable time frame
	- Was not finished in time to be used in the war effort
- Its first task was to perform a series of calculations that were used to help determine the feasibility of the hydrogen bomb
- Continued to operate under BRL management until 1955 when it was disassembled

![](_page_64_Picture_12.jpeg)

### ENIAC

![](_page_65_Figure_1.jpeg)

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#### ENIAC

![](_page_66_Picture_1.jpeg)

![](_page_66_Picture_2.jpeg)

#### John von Neumann

EDVAC (Electronic Discrete Variable Computer)

- First publication of the idea was in 1945
- Stored program concept
	- Attributed to ENIAC designers, most notably the mathematician John von Neumann
	- Program represented in a form suitable for storing in memory alongside the data
- IAS computer
	- Princeton Institute for Advanced Studies
	- Prototype of all subsequent general-purpose computers
	- Completed in 1952

![](_page_67_Picture_10.jpeg)

#### Structure of von Neumann Machine

![](_page_68_Figure_1.jpeg)

Figure 2.1 Structure of the IAS Computer

![](_page_68_Picture_3.jpeg)

## IAS Memory Formats

- The memory of the IAS consists of 1000 storage locations (called words) of 40 bits each
- Both data and instructions are stored there
- Numbers are represented in binary form and each instruction is a binary code

![](_page_69_Figure_4.jpeg)

(b) Instruction word

**Figure 2.2 IAS Memory Formats** 

![](_page_69_Picture_7.jpeg)

## Structure of IAS Computer

#### **Registers**

- Memory Buffer Register (MBR)
	- Word to be stored/received in/from memory or I/O unit
- Memory Address Register (MAR)
	- Memory Address of the word to be (written from)/(read into) the MBR
- Instruction Register (IR)
	- Contains 8-bit opcode
- Instruction Buffer Register (IBR)
	- Temporarily holds the right-hand instruction
- Program Counter (PC)
	- Contains address of the next instruction pair to be fetched from memory
- Accumulator (AC) and Multiplier Quotient (MQ)
	- Employed to temporarily hold operands and results of ALU operations

![](_page_70_Figure_14.jpeg)

![](_page_70_Picture_15.jpeg)

![](_page_71_Picture_23.jpeg)

Table 2.1

The IAS Instruction Set

Table 2.1: The IAS Instruction Set

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![](_page_71_Picture_4.jpeg)
• What would the machine code instruction look like to add the contents of memory address 5CD (HEX) with the accumulator and stores the result back into the accumulator?





### Figure 2.4 Partial Flowchart of IAS Operation





### Figure 2.4 Partial Flowchart of IAS Operation



• What is the assembly language code for the program:





NOTE: IAS doesn't actually have an assembly language



• What is the assembly language code for the program:







- Write an IAS program to compute the results of the following equation:  $Y =$  $N(N + 1)$ 2
- Assume that the result of the computation doesn't overflow and N is a positive integer



$$
Y = \frac{N(N+1)}{2}
$$





• Write an IAS program to compute the results of the following equation:

$$
Y = \sum_{X=1}^{N} X
$$

• Assume that the result of the computation doesn't overflow, and that X, Y, and N are positive integers



$$
Y = \sum_{X=1}^{N} X
$$



T.

### Homework Problems

• Problems are available on Canvas



### Study Guide Exam $\#1$  — CS 440 Computer Architecture

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February 24, 2021

### Contents



### <span id="page-83-0"></span>1 Lecture 00

#### <span id="page-83-1"></span>1.1 Matrices

#### Example Usage

 $a = [12; 21]$ % 1 2 % 2 1 a ∗ a % 5 4 % 4 5

- 1. Matrix multiplication is not commutative
- 2. Inverse function is the same as division
- 3. Cannot invert all matrices (only with determinant not equal to 0)
- 4. System of equations can be solved
- 5. Ranges follow this pattern "begin:step:end"
- 6. Steps can be any decimal value

### <span id="page-84-0"></span>2 Lecture 01

- 1. Difference between architecture and organization
	- Architecture: Specifications of the system being built, which are a set of rules/methods. These describe the functionality, organization and implementation of computer systems.
	- Organization: Deals with the hardware components of a computer system, which include I/O devices, the CPU, storage and primary memory devices (RAM).
- 2. Four structural components for computer:
	- CPU
	- Volatile Memory (RAM)
	- $\bullet$  I/O
	- System Interconnections
- 3. Four structural components for computer:
	- Control Unit (CU)
	- Arithmetic Logic Unit (ALU)
	- Registers
	- $\bullet\,$  CPU Interconnections

#### <span id="page-85-0"></span>3 Lecture 02

- 1. Performance Assessment
	- Qualitative: relating to the possession of qualities without reference to the quantities involved
	- Quantitative: relating to a measurable and numeric representation of a given entity (this is how we gauge the performance of a chipset)
- 2. CPU Time:  $\frac{\text{Clock cycles for a program (cycles)}}{\text{Clock Frequency (cycles/sec)}}$ . The amount of time it takes for a CPU to complete a given set of instructions.
- 3. CPI: Cycles Per Instruction
- 4. IPC: Instructions Per Cycle (inverse of CPI)
- 5. MIPS: Million(s) of Instructions per Second
- 6. MFLOPS: Million(s) of Floating Point Operations Per Second
- 7. For benchmarks however, this will not suffice as it is hard to see which machine is faster

#### <span id="page-85-1"></span>3.1 Benchmark Types

- 1. Total Execution Rate: If Program A and B have equal amount of instructions, you can sum them up individually
- 2. Average Execution Rate: When Program A and B have an unequal amount of instructions
- 3. Harmonic Mean: The reciprocal of the arithmetic mean of the reciprocals. Alternative to average execution rate.
- 4. SPEC Benchmark: Measures the ability of a computer to complete a single task.

$$
r_i = \frac{\text{Tref}_i}{\text{Tsut}_i}
$$

- Tre $f_i$  execution time of benchmark program i on the reference system
- Tsut<sub>i</sub> execution time of benchmark program i on the system under test
- The larger the ratio, the higher the speed

#### <span id="page-86-0"></span>3.2 Amdahl's Law

Adding more processors does not make the program execution time improve.

 $Speedup = Execution time before enhancement  
Execution time after enhancement$ 

[Good Video Explanation](https://www.youtube.com/watch?v=WdRiZEwBhsM)

The more of the code that is running on multiple processors, it will speed up, but it will become saturated.

#### <span id="page-86-1"></span>4 Lecture 03

- 1. ENIAC does not use binary number
- 2. Binary only has 1's and 0's
- 3. Can utilize left/right bit shifts (dividing/multiplying by 2), boolean executions
- 4. You can't use this with decimal numbers (base 10)
- 5. It never had any memory, so programs could not be stored
- 6. Von Neumann machines has same four components of computer
- 7. IAS Memory formats, which hold 40 bits and both instructions/data are stored
	- Left Hand Side
	- Opcode: 0 7
	- Address: 8 19
	- Right Hand Side
	- Opcode: 20 27
	- Address: 28 39

### **Registers**

 $\bullet$ 

- **Memory Buffer Register (MBR)**  $\bullet$ 
	- Word to be stored/received in/from memory or  $\bullet$ I/O unit
- **Memory Address Register (MAR)**  $\bullet$ 
	- Memory Address of the word to be (written from)/(read into) the MBR
- **Instruction Register (IR)** 
	- Contains 8-bit opcode
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	- Temporarily holds the right-hand instruction
- Program Counter (PC)  $\bullet$ 
	- Contains address of the next instruction pair to be  $\bullet$ fetched from memory
- $\bullet$ **Accumulator (AC) and Multiplier Quotient**  $(MQ)$ 
	- Employed to temporarily hold operands and  $\bullet$ results of ALU operations

